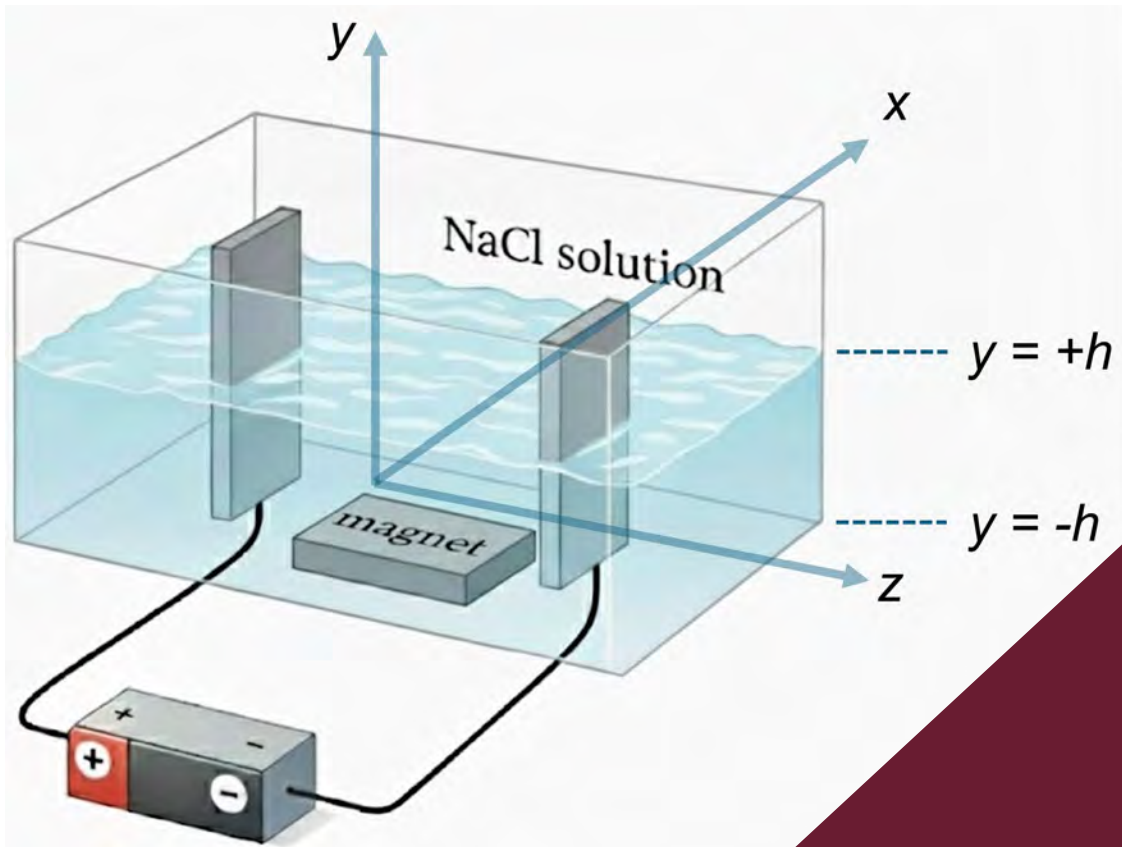


# A table-top demonstration of magnetohydrodynamic flow



Dr. Kausik S Das  
*University of Maryland  
Eastern Shore, MD*

Dr. P Panchadhyayee,  
*Prabhat Chandra College, India*

Sanjoy Pal,  
*Midnapore College, India*



# A table-top demonstration of magnetohydrodynamic flow

- What is Magnetohydrodynamic (MHD) flow?



# A table-top demonstration of magnetohydrodynamic flow

- What is Magnetohydrodynamic (MHD) flow?

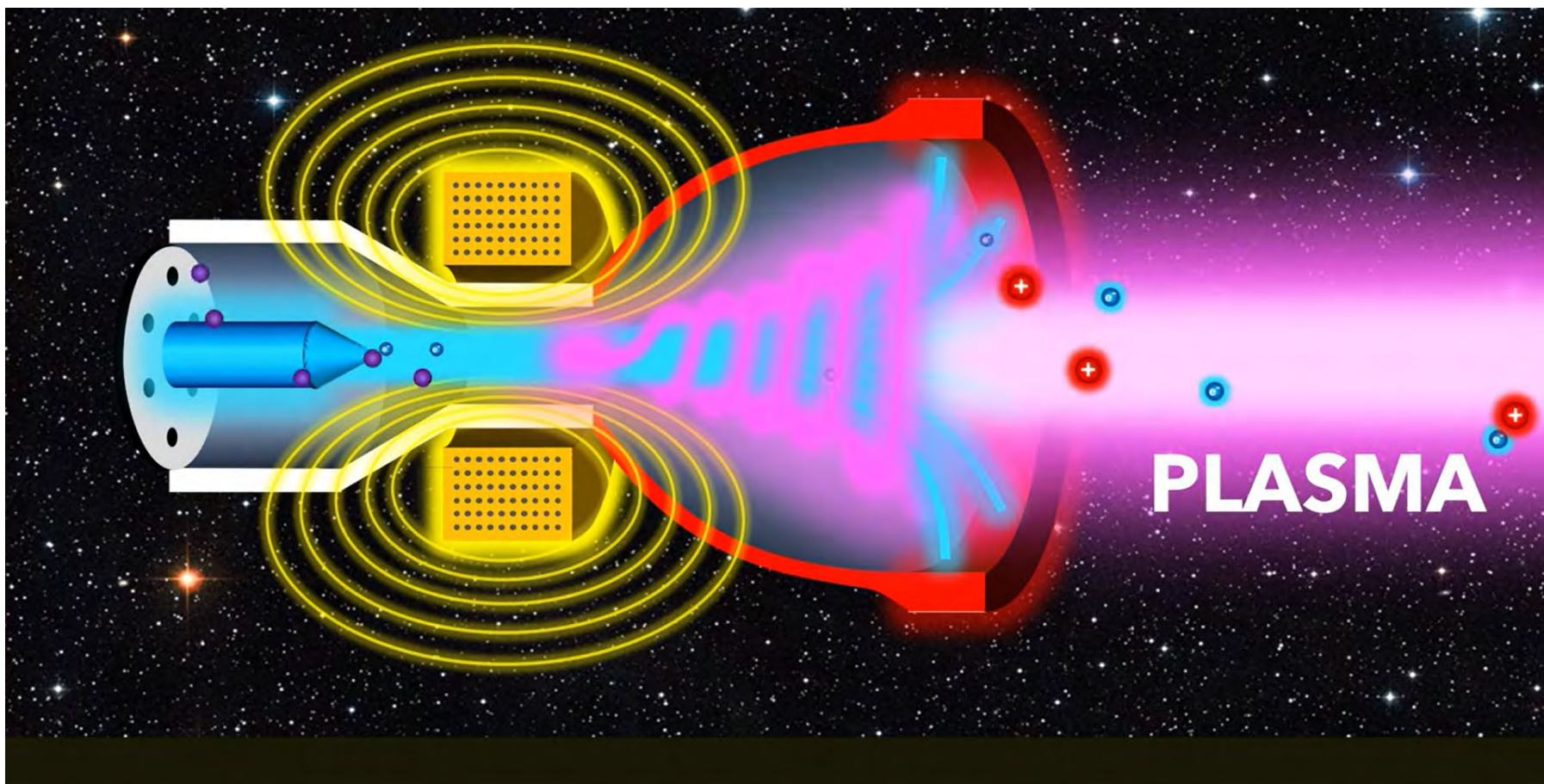
Magnetohydrodynamic (MHD) flow, arises from the interaction between electric currents and magnetic fields in conducting fluids.



UNIVERSITY OF MARYLAND  
EASTERN SHORE

# Applications of MHD flow

- Magnetoplasmadynamic (MPD) thrusters

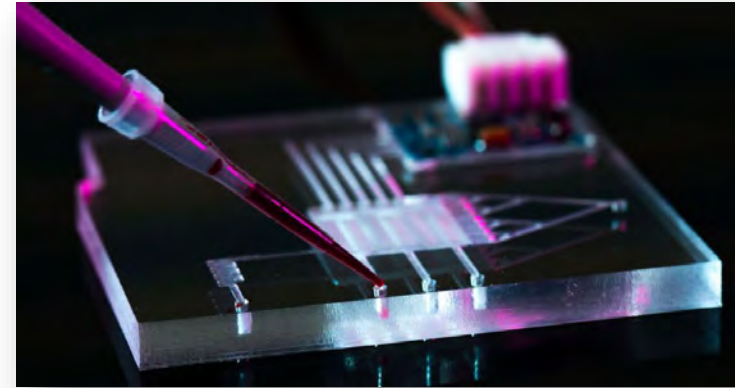
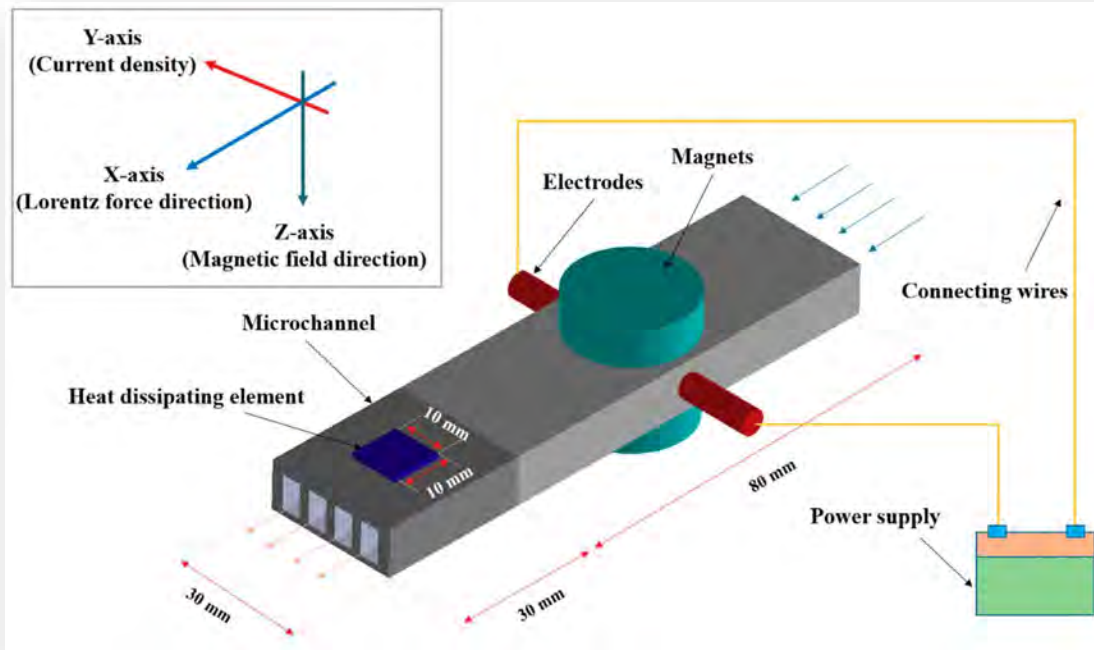




UNIVERSITY OF MARYLAND  
EASTERN SHORE

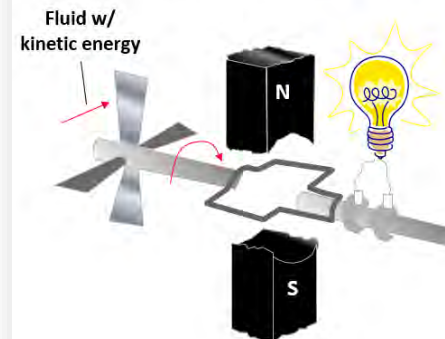
# Applications of MHD flow

- Microfluidics and lab-on-chip systems
- Metallurgy and crystal growth
- Nuclear and fusion systems
- Power generation



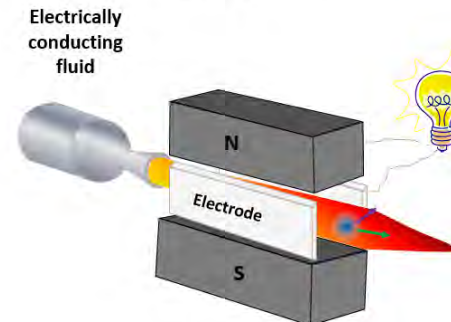
## Turbogenerator

Moving parts limit temperature



## MHD Generator

Electrons **directly extracted** from working fluid itself



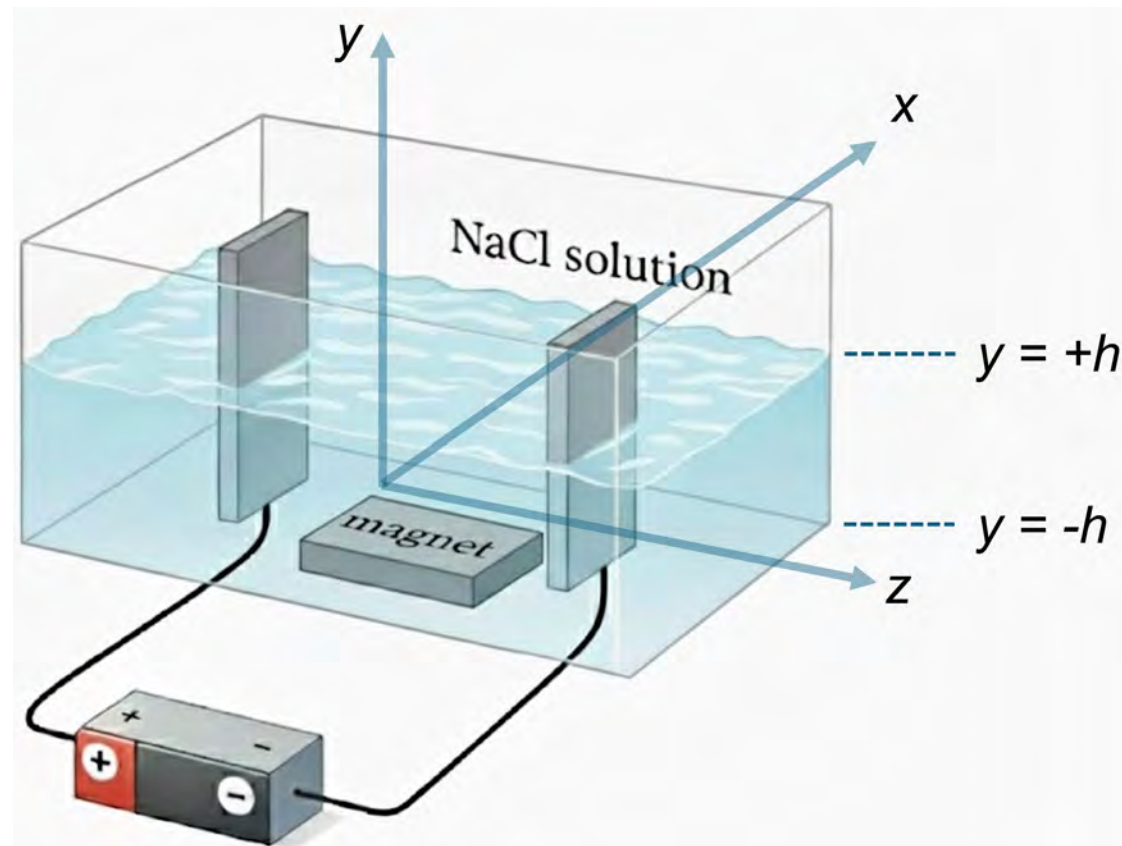
$$P \propto \sigma u^2 B^2$$

$P$ : Generated Power  
 $\sigma$ : Fluid conductivity  
 $u$ : Fluid velocity  
 $B$ : Magnetic field

# A table-top demonstration of magnetohydrodynamic flow

## Defining the geometric coordinate space

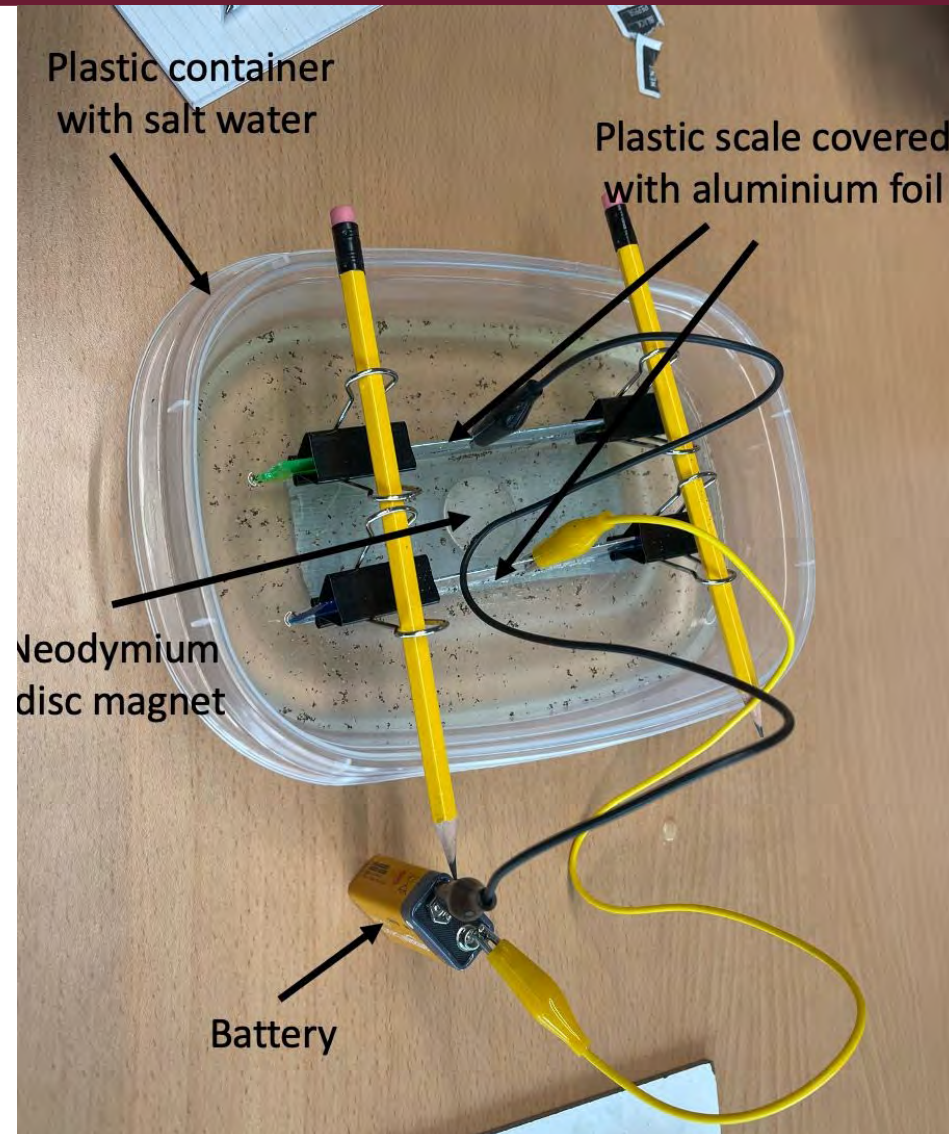
To solve for the flow, we establish an orthonormal coordinate system. The base mean flow is purely streamwise and varies only with wall-normal position  $y$ , such that  $U(y) = U(y)\mathbf{e}_x$ .





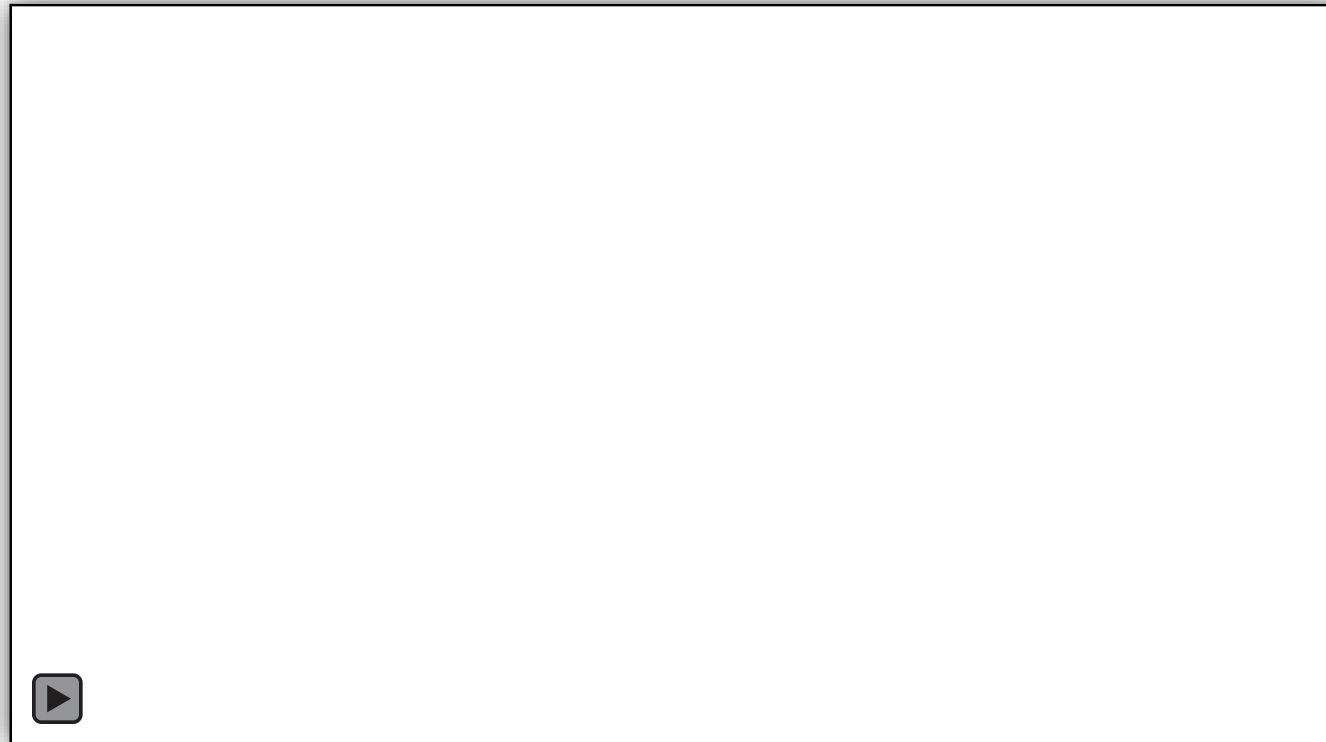
UNIVERSITY OF MARYLAND  
EASTERN SHORE

# A table-top demonstration of magnetohydrodynamic flow






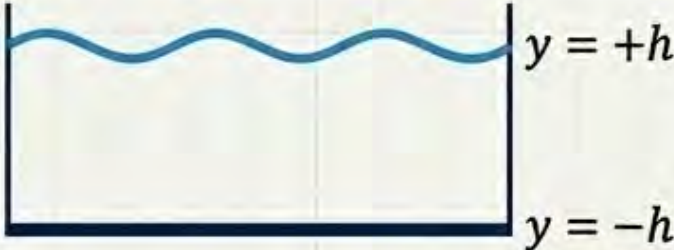
# A table-top demonstration of magnetohydrodynamic flow



# A table-top demonstration of magnetohydrodynamic flow

## The boundary condition pivot

Why standard Hartmann flow theory fails to predict our experimental results.

Standard Closed Channel	Our Asymmetric Experiment
	
<p><b>Lower Boundary:</b> No-slip (<math>y = -h</math>) <math>\rightarrow U(-h) = 0</math></p>	<p><b>Lower Boundary:</b> No-slip (<math>y = -h</math>) <math>\rightarrow U(-h) = 0</math></p>
<p><b>Upper Boundary:</b> No-slip (<math>y = +h</math>) <math>\rightarrow U(+h) = 0</math></p>	<p><b>Upper Boundary:</b> Stress-free / Open (<math>y = +h</math>). Zero viscous traction (<math>\tau_{xy} = \eta dU/dy = 0</math>). <b>Flow Constraint:</b> <math>dU/dy</math> at <math>y=+h = 0</math></p>



# A table-top demonstration of magnetohydrodynamic flow

## Defining the boundary value problem

We seek to solve the differential equation for the velocity profile  $U(y)$ :

Viscous Forces ← Magnetic Dampening/Drive →

$$\eta \frac{d^2 U}{dy^2} - \sigma B_0^2 U - \sigma B_0 E_z = 0$$

Boundary Conditions

$U(-h) = 0$   
(Bottom no-slip constraint)

$dU/dy$  at  $y=+h = 0$   
(Top stress-free constraint)

Key Parameters Defined

$U_E = -E_z/B_0$   
(Electric drift speed)

$Ha = B_0 h \sqrt{\sigma/\eta}$   
(Hartmann number)



# Questions?



UNIVERSITY OF MARYLAND  
EASTERN SHORE



**UNIVERSITY OF MARYLAND  
EASTERN SHORE**